

## MATH 310: ELEMENTARY LINEAR ALGEBRA (FALL 2014)

**Course number:** MAT 310-01

**Course title:** Elementary Linear Algebra

**Credits:** 3

**Meetings:** MWF 12:00–12:50 PM, Petty 217

**Prerequisites:** Grade of C or better in MAT 292

**Instructor information:**

Instructor: Dr. Dan Yasaki [d\\_yasaki@uncg.edu](mailto:d_yasaki@uncg.edu)

Homepage: [http://www.uncg.edu/math/faculty/d\\_yasaki/teaching.html](http://www.uncg.edu/math/faculty/d_yasaki/teaching.html)

Office Hours (146 Petty): MWF 10:00–11:00 AM

**For whom planned:** Mathematics majors and minors

**Catalog description:** Linear systems, matrices, determinants, eigenvalues and eigenvectors, finite-dimensional vector spaces, linear transformations.

**Student learning outcomes:** Upon successful completion of this course students shall be able to

**SLO 1: define** basic terms associated with Linear Algebra, such as linear systems, linear transformations, matrices, linear independence, dimension, rank, null space, basis, vector space, eigenvalues/eigenvectors and orthogonality;

**SLO 2: give examples** of spaces, linear maps or matrices exhibiting properties outlined in SLO 1 in addition to examples of diagonal matrices, invertible matrices, change of bases, and other topics;

**SLO 3: explain** definitions and give precise statements of important theorems of Linear Algebra; and

**SLO 4: construct and defend** coherent mathematical proofs of statements in Linear Algebra based on definitions and previous theorems.

**Teaching methods and assignments for achieving learning outcomes:**

**Reading:** Reading the sections we discuss before class is essential if you wish to get the most out of lectures. This allows you to form questions before you see me present the material so that you can focus on the confusing aspects of the topics we discuss. (SLO 1)

**Lectures:** This is the primary method of content delivery. I plan to follow the book closely, but I will supplement the book's material with some of my own when questions arise or when I feel it is appropriate. (SLO 1–3)

**Quizzes:** There will be short weekly quizzes where you should expect one or two problems – one asking you to state a definition or result and the second asking you to apply that definition or result in some way. (SLO 1–3)

**Tests:** Tests serve as the primary gauge of evaluation. (SLO 1–4)

**Homework:** Homework is the most important way to actually “learn” mathematics.

This is the same sort of practice that is used to learn to play tennis or learn to play the piano. One cannot learn these things by watching them on television or reading about them in a book no more than one can learn mathematics by watching a lecture or reading a mathematics book. (SLO1–4)

**Evaluation and grading:** Semester averages are rounded to the nearest point, and letter grades are assigned on a 10 point scale.

A+ : 97–100	B+ : 87–89	C+ : 77–79	D+ : 67–69
A : 93–96	B : 83–86	C : 73–76	D : 63–66
A– : 90–92	B– : 80–82	C– : 70–72	D– : 60–62

**Homework:** Homework will be collected often. All assignments are weighted equally.

Homework counts for 12.5% of your final grade. Due dates are posted on website.

**Quizzes:** There will be a weekly quiz. All quizzes are weighted equally. Quizzes count for 12.5% of your final grade.

**Tests:** Three tests count 15% of your grade each. The final exam counts for 30% of your final grade.

- (1) Test 1 (Wednesday, September 17)
- (2) Test 2 (Monday, October 20)
- (3) Test 3 (Monday, November 24)
- (4) Final exam (Friday, December 5, noon–3 PM)

**Required text:**

Lay, David C. *Linear Algebra and its Applications*, 4<sup>th</sup> ed., Pearson, 2012. ISBN 13: 978-0-321-38517-8.

**Academic Integrity Policy:** Each student is required to sign the Academic Integrity Policy on all major work submitted for the course.

*I have abided by the UNCG Academic Integrity Policy on this assignment.*

Signature \_\_\_\_\_ Date \_\_\_\_\_

More information can be found at

<http://sa.uncg.edu/handbook/academic-integrity-policy/>.

**Attendance Policy:** Attendance is mandatory. Two consecutive absences or four total absences during the semester may result in a failing grade, regardless of semester average. Attendance will be measured using quizzes.

**Additional information:**

- (1) Students with Disabilities: If you have a documented disability and wish to discuss academic accommodations, please contact me as soon as possible. You are responsible for contacting the OARS in 215 EUC (334-5440, <http://ods.dept.uncg.edu/>) and for arranging the necessary forms for me to fill out and sign. Without these forms the services provided by the OARS will not be available. OARS cannot schedule or reschedule tests without consent from the instructor.

(2) Assignments Policy:

- (a) Assignments are due at the beginning of class. Late assignments will be accepted as late as 5 PM on the due date for half credit and not accepted after that.
- (b) Written assignments must be
  - (i) legible.
  - (ii) stapled (if more than one page).
  - (iii) not torn from a spiral bound notebook.

(3) Absence Policy: You are responsible for all missed material. Any missed assignment, test, or final exam will result in a score of 0. Make-up tests and final exam will be given only if you receive prior approval for a valid excuse by contacting me at least one week in advance.

(4) Copyright Policy: Selling or purchasing notes from classes for commercial gain is a violation of the UNCG Copyright Policy.

<http://policy.uncg.edu/copyright/>

Any student who sells notes taken in class for commercial gain, or who purchases notes taken by another student for commercial gain, is in violation of this policy and, by extension, is committing a violation of the Student Code of Conduct.

<http://sa.uncg.edu/handbook/student-code-of-conduct/>

(5) Email Policy: All email correspondence should be made using your UNCG email account. You must check your email regularly for updates and announcements.

(6) Calculators are not allowed on tests, quizzes, or the final exam. There will be homework exercises that require the use of MATLAB or similar software.

Tentative Calendar					
Week of	Topics			Notes	
1 8/18	1.1	1.2	1.3	Last day to change the course: Friday	
2 8/25	1.4	1.5	1.7		
3 9/1	–	1.8	1.9	Labor Day: Monday	
4 9/8	2.1	2.2	2.3	Class meets in <b>Petty 150</b> this week.	
5 9/15	Review	Test 1	2.8	<b>Test 1</b> (1.1–2.3): Wednesday	
6 9/22	2.9	3.1, 3.2	3.3		
7 9/29	4.1	4.2	4.3		
8 10/6	4.4	4.5	4.6	Last day to withdraw: Friday	
9 10/13	–	4.7	Review	Fall Break: Monday	
10 10/20	Test 2	5.1	5.2	<b>Test 2</b> (2.8–4.7): Monday	
11 10/27	5.3	5.4	5.5		
12 11/3	5.6	5.8	Review		
13 11/10	6.1	6.2	Review		
14 11/17	6.3	6.5	Review		
15 11/24	Test 3	–	–	<b>Test 3</b> (5.1–6.5): Monday Thanksgiving break	
16 12/1	Review	–	Final	Last day: Monday <b>Final Exam</b> (1.1–6.5): Friday, noon–3PM	

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## 1. Linear Equations in Linear Algebra

- 1.1 Systems of Linear Equations (1–4, 8, 10, 12, 20–25)
- 1.2 Row Reduction and Echelon Forms (2–16 (even), 20–27, 30, 31)
- 1.3 Vector Equations (8, 12–16 (even), 22–25)
- 1.4 The Matrix Equation  $\mathbf{Ax} = \mathbf{b}$  (2–20 (even), 23, 24–32 (even))
- 1.5 Solution Sets of Linear Systems (2–14 (even), 23–26, 28–36 (even), 37)
- 1.7 Linear Independence (2–20 (even), 21–30, 34, 38)
- 1.8 Introduction to Linear Transformations (4, 6, 9, 10, 13–16, 18, 20, 21–24)
- 1.9 The Matrix of a Linear Transformation (2, 4, 16, 23–27, 31–36)

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## 2. Matrix Algebra

- 2.1 Matrix Operations ((6–12) even, 13, 15, 16, 18–22, 28, 29, 32)
- 2.2 The Inverse of a Matrix (8–11, 12–24 (even), 35)
- 2.3 Characterization of Invertible Matrices (2–10 (even), 11–14, 18–25)
- 2.8 Subspaces of  $\mathbb{R}^n$  (2–8 (even), 16, 18, 20–22, 24, 26 )
- 2.9 Dimension and Rank (2–16 (even), 17, 18, 22, 24, 25, 27)

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## 3. Determinants

- 3.1 Introduction to Determinants (2–8 (even), 16–26 (even), 34, 39, 40)
- 3.2 Properties of Determinants (2–10 (even), 16, 18, 22, 27, 28, 31, 35)
- 3.3 Cramer’s Rule, Volume, and Linear Transformations (20, 22, 26–32)

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## 4. Vector Spaces

- 4.1 Vector Spaces and Subspaces (2–18 (even), 23, 24, 32, 33)
- 4.2 Null Spaces, Column Spaces, and Linear Transformations (4–24 (even), 25, 26, 32, 33, 34\*, 35\*)
- 4.3 Linearly Independent Sets; Bases (2–8 (even), 12, 16, 21–25, 31, 32\*)
- 4.4 Coordinate Systems (2, 4, 12, 15–17, 23, 24, 28, 31\*, 33\*)
- 4.5 The Dimension of a Vector Space (2, 4, 8, 12, 18, 19, 20, 24, 29, 30, 32\*)
- 4.6 Rank (2, 4, 5–16 (even), 17, 18, 20, 28, 30, 34\*)
- 4.7 Change of Basis (6, 8, 11, 12, 14, 17\*, 18\*)

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## 5. Eigenvalues and Eigenvectors

- 5.1 Eigenvectors and Eigenvalues (2, 4, 6, 14, 20, 21, 22, 31, 32)
- 5.2 The Characteristic Equation (2, 8, 10, 19, 20, 21, 22, 24)
- 5.3 Diagonalization (2, 4, 8, 12, 21, 22, 31, 32)
- 5.4 Eigenvectors and Linear Transformations (2, 4, 10, 12, 20, 25, 26, 30)
- 5.5 Complex Eigenvalues (2, 6, 12, 14, 23, 24)
- 5.6 Discrete Dynamical Systems (1, 2, 3, 5, 10, 17)
- 5.8 Iterative Estimates for Eigenvalues (1–6, 13–16)

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## 6. Orthogonality and Least Squares

- 6.1 Inner Product, Length, and Orthogonality (2–14 (even), 19–30)
- 6.2 Orthogonal Sets (2–16 (even), 23–29, 31, 33)
- 6.3 Orthogonal Projections (2–14 (even), 21–24)
- 6.5 Least-Squares Problems (2–14 (even), 17–19)

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