

## MAT 514: Theory of Numbers independent study (Fall 2012)

**Course number:** MAT 514

**Course title:** Theory of Numbers independent study (Fall 2012)

**Credits:** 3

**Prerequisites:** Permission of instructor.

**Instructor information:**

Instructor: Dr. Dan Yasaki [d\\_yasaki@uncg.edu](mailto:d_yasaki@uncg.edu)

Homepage: [http://www.uncg.edu/math/faculty/d\\_yasaki/teaching.html](http://www.uncg.edu/math/faculty/d_yasaki/teaching.html)

Office Hours (146 Petty): Mondays 8:30 - 9:30 AM, Tuesdays & Thursdays 11:00 - noon

**For whom planned:** Abhishek Pratap

**Catalog description:** An introductory course to both multiplicative and additive number theory. Divisibility, prime numbers, congruencies, linear and nonlinear Diophantine equations (including Pell's equation), quadratic residues, number-theoretic functions, and other topics.

**Student learning outcomes:** Upon successful completion of this course, students will be able to:

- define the fundamental terms in elementary number theory.
- explain how RSA encryption allows for secure message transcription.
- combine definitions and results to create rigorous proofs of basic statements about elementary number theory.
- evaluate an argument for logical validity.

**Teaching methods and assignments for achieving learning outcomes:** The student will read and work through the course material independently. Achievement of learning outcomes will be facilitated via homework assignments/weekly presentations by the student and the final exam.

**Evaluation and grading:** Semester averages are rounded to the nearest point, and letter grades are assigned on a 10 point scale.

A+ : 97–100	B+ : 87–89	C+ : 77–79	D+ : 67–69
A : 93–96	B : 83–86	C : 73–76	D : 63–66
A– : 90–92	B– : 80–82	C– : 70–72	D– : 60–62

- Weekly homework presentations (70%)
- Final exam (30%)

**Required text:**

- Textbook: *Elementary Number Theory: Primes, Congruences, and Secrets* available at <http://wstein.org/ent/>

**Topical outline:**

- Divisibility and greatest common divisors
- Modular arithmetic
- Prime numbers and unique factorization
- Primitive roots
- Diffie-Hellman key exchange
- Chinese remainder theorem
- Euler's formula
- Diophantine equations
- RSA public key cryptosystem
- Factorization techniques
- Quadratic residues and quadratic reciprocity
- Additional topics such as elliptic curve cryptography if time permits.

**Academic Integrity Policy:** Each student is required to sign the Academic Integrity Policy on all major work submitted for the course.

*I have abided by the UNCG Academic Integrity Policy on this assignment.*

Signature \_\_\_\_\_ Date \_\_\_\_\_

More information can be found at <http://academicintegrity.uncg.edu/complete/>.

**Final examination:** The Final Exam covers the entire semester. The time and date will be announced later in the semester.